

Formule trigonometrice

1. $\cos^2 x + \sin^2 x = 1,$
2. $1 + \operatorname{tg}^2 x = \frac{1}{\cos^2 x} \quad x \neq \frac{\pi}{2} + k\pi,$
3. $1 + \operatorname{ctg}^2 x = \frac{1}{\sin^2 x}, \quad x \neq k\pi.$
4. $\sin(x \pm y) = \sin x \cdot \cos y \pm \sin y \cdot \cos x;$
5. $\cos(x \pm y) = \cos x \cdot \cos y \mp \sin x \cdot \sin y;$
6. $\sin 2x = 2\sin x \cdot \cos x;$
7. $\cos 2x = \cos^2 x - \sin^2 x$ din care rezulta:
8. $\cos 2x = 2\cos^2 x - 1; \quad \cos 2x = 1 - 2\sin^2 x$ si
9. $|\cos x| = \sqrt{\frac{1 + \cos 2x}{2}}; \quad |\sin x| = \sqrt{\frac{1 - \cos 2x}{2}}.$

Alte formule:

10. $\operatorname{tg}(x \pm y) = \frac{\operatorname{tg} x \pm \operatorname{tg} y}{1 \mp \operatorname{tg} x \operatorname{tg} y}; \quad \operatorname{ctg}(x \pm y) = \frac{\operatorname{ctg} x \cdot \operatorname{ctg} y \mp 1}{\operatorname{ctg} y \pm \operatorname{ctg} x};$
11. $\operatorname{tg} 2x = \frac{2\operatorname{tg} x}{1 - \operatorname{tg}^2 x}; \quad \operatorname{ctg} 2x = \frac{\operatorname{ctg}^2 x - 1}{2\operatorname{ctg} x};$
12. $\operatorname{tg} \frac{x}{2} = \frac{2\operatorname{tg} \frac{x}{2}}{1 - \operatorname{tg}^2 \frac{x}{2}}; \quad \sin x = \frac{2\operatorname{tg} \frac{x}{2}}{1 + \operatorname{tg}^2 \frac{x}{2}}; \quad \cos x = \frac{1 - \operatorname{tg}^2 \frac{x}{2}}{1 + \operatorname{tg}^2 \frac{x}{2}}.$

Formule de transformare a sumei in produs:

13. $\sin a + \sin b = 2\sin \frac{a+b}{2} \cos \frac{a-b}{2}; \quad \sin a - \sin b = 2\sin \frac{a-b}{2} \cos \frac{a+b}{2};$
14. $\cos a + \cos b = 2\cos \frac{a+b}{2} \cos \frac{a-b}{2}; \quad \cos a - \cos b = -2\sin \frac{a+b}{2} \sin \frac{a-b}{2};$
15. $\operatorname{tg} a + \operatorname{tg} b = \frac{\sin(a+b)}{\cos a \cos b}; \quad \operatorname{tg} a - \operatorname{tg} b = \frac{\sin(a-b)}{\cos a \cos b};$

$$16. \operatorname{ctg} a + \operatorname{ctg} b = \frac{\sin(a+b)}{\sin a \sin b}; \operatorname{ctg} a - \operatorname{ctg} b = \frac{\sin(b-a)}{\sin a \sin b}.$$

Formule de transformarea produsului in suma:

$$17. \sin a \cos b = \frac{\sin(a+b) + \sin(a-b)}{2};$$

$$18. \cos a \cos b = \frac{\cos(a+b) + \cos(a-b)}{2};$$

$$19. \sin a \sin b = \frac{\cos(a-b) - \cos(a+b)}{2}.$$

www.matematicon.ro